

The NANOGrav 12.5 yr Data Set: Bayesian Limits on Gravitational Waves from **Individual Supermassive Black Hole Binaries**

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Abstract

Pulsar timing array collaborations, such as the North American Nanohertz Observatory for Gravitational Waves (NANOGrav), are seeking to detect nanohertz gravitational waves emitted by supermassive black hole binaries formed in the aftermath of galaxy mergers. We have searched for continuous waves from individual circular supermassive black hole binaries using NANOGrav's recent 12.5 yr data set. We created new methods to accurately model the uncertainties on pulsar distances in our analysis, and we implemented new techniques to account for a common red-noise process in pulsar timing array data sets while searching for deterministic gravitational wave signals, including continuous waves. As we found no evidence for continuous waves in our data, we placed 95% upper limits on the strain amplitude of continuous waves emitted by these sources. At our most sensitive frequency of 7.65 nHz, we placed a sky-averaged limit of $h_0 < (6.82 \pm 0.35) \times 10^{-15}$, and $h_0 < (2.66 \pm 0.15) \times 10^{-15}$ in our most sensitive sky location. Finally, we placed a multimessenger limit of $\mathcal{M} < (1.41 \pm 0.02) \times 10^9 M_{\odot}$ on the chirp mass of the supermassive black hole binary candidate 3C 66B.

Unified Astronomy Thesaurus concepts: Gravitational waves (678); Astronomy data analysis (1858); Millisecond pulsars (1062); Supermassive black holes (1663)

1. Introduction

Supermassive black hole binaries (SMBHBs) are expected to form in the aftermath of galaxy mergers, when the two constituent supermassive black holes eventually become gravitationally bound (Begelman et al. 1980). If they are able to reach an advanced stage of evolution, with subparsec orbital separations, these binaries are predicted to be among the brightest sources of low-frequency gravitational waves (GWs) in the universe, emitting at frequencies of $\sim 10^{-9}$ to 10^{-7} Hz. The GWs emitted by discrete SMBHBs are known as continuous waves (CWs) owing to their minimal frequency evolution, while the dominant source of nanohertz GWs is expected to be the stochastic GW background (GWB) that has contributions from the entire cosmic population of SMBHBs and potentially other sources (Sesana et al. 2004; Burke-Spolaor et al. 2019).

By carefully monitoring the radio pulses from stable millisecond pulsars over many years, pulsar timing arrays (PTAs) should be able to detect correlated fluctuations in the pulse times of arrival (TOAs) owing to the influence of low-frequency GWs (Detweiler 1979; Foster & Backer 1990). There are multiple PTA collaborations currently operating; among them, the North American Nanohertz Observatory for Gravitational Waves (NANOGrav; McLaughlin 2013), the Parkes PTA (PPTA; Hobbs 2013, 2013), and the European PTA (EPTA; Desvignes et al. 2016) have each produced multiple pulsar timing data sets that have been searched for GWs. These groups, along with other pulsar timing projects, combine efforts as a consortium known as the International PTA (IPTA; Verbiest et al. 2016).

These PTA data sets have enabled numerous searches for GWs from SMBHBs, as well as primordial GWs (e.g., Vagnozzi 2021; Benetti et al. 2022), cosmic strings (e.g., Arzoumanian et al. 2018), and cosmological phase transitions (Arzoumanian et al. 2021a; Xue et al. 2021). Modeling has

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Original content from this work may be used under the terms of the Creative Commons Attribution 4.0 licence. Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI. suggested that the GWB signal from SMBHBs will be detected first (Rosado et al. 2015). While PTAs have not yet detected a GWB, they have placed steadily improving limits on such a signal (van Haasteren et al. 2011; Demorest et al. 2013; Shannon et al. 2013, 2015; Lentati et al. 2015; Arzoumanian et al. 2016, 2018; Verbiest et al. 2016) until around 2015, when published limits began to stabilize at a characteristic strain value of a few times 10^{-15} . In the NANOGrav 12.5 yr data set (Alam et al. 2021a), PPTA second data release (Kerr et al. 2020), EPTA data release 2 (Chen et al. 2021), and IPTA data release 2 (Perera et al. 2019), not only does the upper limit no longer decrease, but a common red-noise (CRN) process with characteristics similar to those predicted for an SMBHB-origin GWB was detected to high significance, albeit without evidence for the specific spatial correlation assumed for the GWB (Arzoumanian et al. 2020a; Goncharov et al. 2021; Antoniadis et al. 2022; Falxa et al. 2023). Significant effort has been dedicated to determining whether the CRN is an early warning sign of a future GWB detection (Pol et al. 2021) or an anomaly due to pulsar noise modeling (Zic et al. 2022) and to the development of validity tests to determine between these two scenarios (Goncharov et al. 2022), but more data are required to make a final determination.

While this CRN process is heartening for future GWB searches (Pol et al. 2021), it has sparked new challenges for CW searches, as the background takes the form of a noise process, which (like any noise process underlying a signal) will work to disrupt the sensitivity of CW searches. Over the past decades, all-sky and allfrequency CW searches have improved their sensitivity by several orders of magnitude in GW strain (e.g., Yardley et al. 2010; Arzoumanian et al. 2014; Zhu et al. 2014; Babak et al. 2016; Aggarwal et al. 2019), allowing the sensitivity horizon of PTAs to expand by several orders of magnitude. This has allowed the PTA horizon to include increasing numbers of specific systems of interest (e.g., Lommen & Backer 2001; Jenet et al. 2004; Aggarwal et al. 2019; Charisi et al. 2022). PTAs are likely to reach the sensitivities required to detect a CW soon after the GWB is detected, with recent studies suggesting that this will occur in the next 5–10 yr (Rosado et al. 2015; Mingarelli et al. 2017; Kelley et al. 2018; Bécsy et al. 2022b). Additionally, we are working to revise and improve CW search methodologies through

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search speed-ups (Bécsy et al. 2022a) and efficient sampling techniques (Aggarwal et al. 2019) as CW upper limits decrease. In this paper, we present the results of an all-sky search for CWs from individual circular SMBHBs in the NANOGrav 12.5 yr data set. This work is an extension of the searches performed in previous NANOGrav data sets (presented in Arzoumanian et al. 2014 and Aggarwal et al. 2019 for the 5 and 11 yr data sets, respectively) and uses analogous techniques to

the search for CWs in the IPTA data release 2 (Falxa et al. 2023). Our new search benefited from the use of the more sensitive 12.5 yr data set. Most critically, however, in this work we needed to account for the existence of an emerging common-noise signal in this data set, and we understand the impact that this signal may have on CW sensitivity.

This paper is organized as follows. In Section 2, we present an overview of the data used for our analysis, details of new pulsar distance modeling methods created for CW searches, and a description of the GW signals and analysis methods used throughout this paper. In Section 3, we present the results of our GW searches. In Section 4, we interpret their broader astrophysical context. For the busy reader, our main results can be summarized as follows:

- 1. For accurate low-frequency CW searches, the CRN that has been seen in GWB searches must be accounted for in our signal modeling; otherwise, our detection metrics may report a false-positive result.
- 2. Once the CRN was taken into account, we found that no CWs were detected in the 12.5 yr data set.
- 3. With this knowledge, we placed stringent limits on the CW amplitude as a function of GW frequency. For the most sensitive frequency of 7.65×10^{-9} Hz, we reach strain 95% upper limits of $h_0 < (6.82 \pm 0.35) \times 10^{-15}$, and we also placed limits on the CW amplitude at this frequency as a function of sky location.
- 4. While our all-sky sensitivity has improved with each subsequent NANOGrav data set, we found herein that for 85% of the sky, the upper limit at the most sensitive frequency of 7.65×10^{-9} Hz is comparable to or worse than in previous data sets. Through extensive simulations that encompass the complex evolution of pulsar noise parameters, ephemeris updates, and Bayesian modeling, we linked this effect to the newly detectable CRN process in the 12.5 yr data set.
- 5. We used these limits to make inferences about the local population of SMBHBs and limited the distance to an SMBHB emitting at 7.65×10^{-9} Hz to be greater than 86.7 Mpc for a $10^9 M_{\odot}$ binary in the most sensitive sky location.
- 6. We used multimessenger techniques to update limits on the chirp mass of the SMBHB candidate 3C 66B to be less than $\mathcal{M} < (1.41 \pm 0.02) \times 10^9 M_{\odot}$ and placed new limits on the chirp mass of SMBHB candidate HS 1630 +2355 to be less than $\mathcal{M} < (1.28 \pm 0.03) \times 10^{10} M_{\odot}$.

In Section 5, we discuss the implications of these results. In Section 6, we summarize our conclusions.

2. Methods

2.1. The 12.5 yr Data Set

We analyzed the NANOGrav 12.5 yr data set, originally published as Alam et al. (2021a, 2021b), which consists of

TOAs and timing models from 47 pulsars. Two versions of the data set were created from the original observations, taken between 2004 and 2017, using independent analyses. Here we make use of the narrowband version of the data set (Alam et al. 2021a). This adds two pulsars and 1.5 yr of observations over the previous 11 yr data set. For GW analyses, we require the pulsars to have a timing baseline of at least 3 yr; therefore, we use only 45 of the 47 pulsars included in the full data set. However, the 11 yr data set included only 34 pulsars that could be used in GW analyses, so this addition, which includes a factor of ~ 1.5 increase in the number of pulse TOAs, represents a significant addition of data, increasing our sensitivity. It is important to note that the 12.5 yr data set is not merely an addition of TOAs to previous releases but a full reanalysis with an updated pipeline, described in detail in Alam et al. (2021a). Thus, our search also benefited from improved timing precision for pulsars shared with previous data sets. However, it is important to note that this reprocessing resulted in new values being measured for each pulsar's noise parameters.

2.2. Signal Model

As in previous NANOGrav searches for continuous GWs, we will describe the effect of an individual SMBHB on a pulsar's TOAs and its timing model. A starting point is the residuals, δt , obtained after subtracting a basic timing model (which excludes noise and GW parameters) from the measured arrival times. While the methods remain nearly identical to previous iterations, slight alterations have been made to improve consistency with other work in the field, to reflect more recent data, and to include the CRN in the CW search. As such, we will lay out the methods with particular focus on any instances that have changed since NANOGrav's most recent CW search (Aggarwal et al. 2019). Note that throughout this paper we use units where G = c = 1, cosmology calculations assume $H_0 = 69.32 \text{ km s}^{-1} \text{ Mpc}^{-1}$, and the GW derivations assume general relativity.

The pulsar residuals can be separated into multiple components as

$$\delta t = M\epsilon + n_{\rm white} + n_{\rm red} + s, \tag{1}$$

where *M* is the design matrix, which describes the linearized timing model, and ϵ is a vector of the timing model parameter offsets. This term allows the timing model parameters of each pulsar to be adjusted in accordance with the presence of any additional signals. The variables n_{white} and n_{red} refer to vectors describing the pulsar white and red noise, respectively, and *s* is a vector of GW-induced signal present in the residuals.

2.2.1. CW Signal

For a GW source located at R.A. α and decl. δ , we define the polar angle $\theta = \pi/2 - \delta$ and azimuthal angle $\phi = \alpha$. The strain of GWs emitted from such a source can be written in terms of two polarizations as

$$h_{ab}(t,\,\hat{\Omega}) = e_{ab}^+(\hat{\Omega})h_+(t,\,\hat{\Omega}) + e_{ab}^\times(\hat{\Omega})h_\times(t,\,\hat{\Omega}),\tag{2}$$

where $\hat{\Omega}$ is a unit vector pointing from the GW source to Earth (along the direction of propagation), $h_{+,\times}$ are the polarization amplitudes, and $e_{ab}^{+,\times}$ are the polarization tensors. These can be

written in the solar system barycenter frame as

$$e_{ab}^{+} = \hat{p}_a \hat{p}_b - \hat{q}_a \hat{q}_b$$
$$e_{ab}^{\times} = \hat{p}_a \hat{q}_b + \hat{q}_a \hat{p}_b$$
(3)

and are constructed from basis vectors,

$$\hat{n} = (\sin\theta\cos\phi, \sin\theta\sin\phi, \cos\theta) = -\hat{\Omega}$$
$$\hat{p} = (\cos\psi\cos\theta\cos\phi - \sin\psi\sin\phi, \cos\psi\cos\theta\sin\phi, -\cos\psi\sin\phi, -\cos\psi\sin\theta)$$
$$\hat{q} = (\sin\psi\cos\theta\cos\phi + \cos\psi\sin\phi, -\cos\psi\sin\theta)$$
$$\hat{q} = (\sin\psi\cos\theta\cos\phi - \cos\psi\cos\phi, -\sin\psi\sin\theta), \quad (4)$$

where ψ is the GW polarization angle. Note that this basis is different from that used in Aggarwal et al. (2019) to maintain better consistency with previous references and the standards used by other GW detectors. Differences can be reduced to a rotation of the frame by an angle equivalent to the GW polarization angle ψ . These polarization tensors are used to construct the antenna pattern function $F^{+,\times}(\hat{\Omega})$, which describes the response of the pulsar (at unit vector \hat{u}) to the GW source, as in Taylor et al. (2016), where

$$F^{A}(\hat{\Omega}) \equiv \frac{1}{2} \frac{\hat{\mu}^{a} \hat{\mu}^{b}}{1 + \hat{\Omega} \cdot \hat{\mu}} e^{A}_{ab}(\hat{\Omega}).$$
(5)

Now we can write the signal *s* induced by the GW as seen in the pulsar's residuals as

$$s(t, \hat{\Omega}) = F^+(\hat{\Omega})\Delta s_+(t) + F^{\times}(\hat{\Omega})\Delta s_{\times}(t), \qquad (6)$$

where $\Delta s_{+,\times}$ is the difference between the signal induced at Earth (the "Earth term") and that induced at the pulsar (the "pulsar term"). This can be written as

$$\Delta s_{+,\times}(t) = s_{+,\times}(t_p) - s_{+,\times}(t), \tag{7}$$

where t and t_p represent the time when the GW passes Earth and the pulsar, respectively. These times can be related geometrically by

$$t_p = t - L(1 + \hat{\Omega} \cdot \hat{u}), \tag{8}$$

where \hat{u} is the line-of-sight vector to the pulsar and *L* is the distance to the pulsar (see Section 2.3.4 for further discussion of this value).

For a circular binary at zeroth post-Newtonian (0-PN) order, $s_{+,\times}$ can be written as

$$s_{+}(t) = \frac{\mathcal{M}^{5/3}}{d_{L}\omega(t)^{1/3}} [-\sin 2\Phi(t)(1 + \cos^{2}t)],$$

$$s_{\times}(t) = \frac{\mathcal{M}^{5/3}}{d_{L}\omega(t)^{1/3}} [2\cos 2\Phi(t)\cos t],$$
(9)

where ι is the inclination angle of the SMBHB, d_L is the luminosity distance to the source, $\omega(t)$ and $\Phi(t)$ are the timedependent angular orbital frequency and phase, respectively, and $\mathcal{M} \equiv (m_1 m_2)^{3/5} / (m_1 + m_2)^{1/5}$ is a combination of the two black hole masses known as the chirp mass. Again, note that the forms of these signals have been reorganized compared to those used in Aggarwal et al. (2019); due to the rotated frame of the antenna pattern functions now in use, they are equivalent. The variables \mathcal{M} and ω refer to the redshifted values of these quantities, which relate to the rest-frame versions \mathcal{M}_r and ω_r as

$$\mathcal{M}_r = \frac{\mathcal{M}}{1+z},$$

$$\omega_r = \omega(1+z).$$
(10)

However, PTAs are currently thought to be sensitive only to individual SMBHBs in the local universe where $(1 + z) \sim 1$.

For a CW, the initial orbital angular ω_0 frequency is related to the GW frequency by $\omega_0 = \pi f_{GW}$, where $\omega_0 = \omega(t_0)$. For this search, we define the reference time t_0 as MJD 57933 (2017 June 29), the date of the last observation for the 12.5 yr data set. The time-dependent orbital phase and frequency of the binary are given by

$$\Phi(t) = \Phi_0 + \frac{1}{32} \mathcal{M}^{-5/3} [\omega_0^{-5/3} - \omega(t)^{-5/3}],$$

$$\omega(t) = \omega_0 \left(1 - \frac{256}{5} \mathcal{M}^{5/3} \omega_0^{8/3} t\right)^{-3/8},$$
(11)

where Φ_0 refers to the initial orbital phase (Arzoumanian et al. 2014). To account for the evolution of high chirp mass binaries over our observations, rather than assuming that there is no frequency evolution, we use the full expression for $\omega(t)$ as in Aggarwal et al. (2019).

2.2.2. Noise Model

For each individual pulsar, we model both white and red noise. We use a white noise model that is identical to that used in previous NANOGrav analyses, using three parameters: EFAC, EQUAD, and ECORR. EFAC scales the template-fitting TOA uncertainties induced by finite pulse signal-to-noise ratios by a multiplicative factor, EQUAD adds white noise in quadrature, and ECORR describes white noise that is correlated across TOAs derived from data collected simultaneously (Lam et al. 2017).

For consistency with previous NANOGrav analyses, to model individual pulsar red noise, the noise spectrum is divided into 30 linearly spaced bins, ranging from $1/T_{obs}$ to $30/T_{obs}$, where T_{obs} is the total observation baseline for each pulsar. Then, the power spectral density of the red noise is fit to a power-law model as in Shannon & Cordes (2010) and Lam et al. (2017), where

$$P(f) = \frac{A_{\text{red}}^2}{12\pi^2} \left(\frac{f}{f_{\text{yr}}}\right)^{-\gamma_{\text{red}}} \text{yr}^3.$$
(12)

Here $f_{yr} \equiv 1/(1 \text{ yr})$, A_{red} is the red-noise amplitude, and γ_{red} is the power-law spectral index. The prior on A_{red} is log-uniform in the range [-20, -11], while the prior on γ is uniform in the range [0, 7].

As mentioned above, for the first time, a CRN signal is now detectable in the 12.5 yr data set (Arzoumanian et al. 2020a). Because of this, we included a CRN term in our signal model for a portion of our analyses, where the CRN amplitude and spectral index are held fixed to those preferred in Arzoumanian et al. (2020a). The results of searches that only model a CW necessitated this addition and are described in detail in

The Astrophysical Journal Letters, 951:L28 (17pp), 2023 July 10

Section 3. The power spectral density of the CRN,

$$P(f) = \frac{A_{\text{CRN}}^2}{12\pi^2} \left(\frac{f}{f_{\text{yr}}}\right)^{-\gamma_{\text{CRN}}} \text{yr}^3, \qquad (13)$$

takes the same form as that of the pulsar red noise in Equation 12, but with an amplitude A_{CRN} and spectral index γ_{CRN} that are common to all of the pulsars in the array.

2.3. Bayesian Methods

We utilized Bayesian inference techniques to determine the posterior distributions of GW parameters. In previous CW analyses (Arzoumanian et al. 2014; Aggarwal et al. 2019), these results were compared to a frequentist metric, the \mathcal{F}_p statistic (Ellis et al. 2012), to confirm our key results. However, as this method does not currently account for a common process other than a CW in the data, more development will be necessary to produce reliable frequentist results on the 12.5 yr data set through the addition of noise marginalization capabilities, similar to Vigeland et al. (2018). Therefore, in this work we will focus solely on the Bayesian searches, and the frequentist analyses will be presented in a future work.

In each analysis, we include the BAYESEPHEM model (Vallisneri et al. 2020) to account for the uncertainties in the solar system ephemeris, which, as first described in Arzoumanian et al. (2018), can have large impacts on the computation of GW upper limits with PTAs. We used DE438 (Folkner & Park 2018) plus BAYESEPHEM to transform from individual observatory reference frames to an inertial frame centered at the solar system barycenter.

As in previous NANOGrav CW searches, we use the enterprise (Ellis et al. 2019) package to construct the priors and evaluate the likelihood, which takes the same form as in Aggarwal et al. (2019) and Arzoumanian et al. (2014). The Markov Chain Monte Carlo (MCMC) sampler package PTMCMCSampler (Ellis & van Haasteren 2017) was used to explore the parameter space. Before analyzing our data, we performed a prior-recovery analysis to ensure that the sampler could search the entire prior volume.

The CW signal model can be described by nine global parameters,

$$\{\theta, \phi, f_{\text{GW}}, \Phi_0, \psi, i, \mathcal{M}, d_L, h_0\},$$
(14)

which describe the circular SMBHB's

- 1. position on the sky (θ, ϕ) ;
- 2. GW frequency, related to the orbital frequency at a reference time (f_{GW});
- 3. orbital phase at a reference time (Φ_0) ;
- 4. GW polarization angle (ψ);
- 5. orbital inclination (ι) ;
- 6. chirp mass (\mathcal{M}) ;
- 7. luminosity distance (d_L) ; and
- 8. strain amplitude (h_0) , which is related to the chirp mass, GW frequency, and luminosity distance.

Since h_0 can be defined as

$$h_0 = \frac{2\mathcal{M}^{5/3} (\pi f_{\rm GW})^{2/3}}{d_I},\tag{15}$$

there is a degeneracy between h_0 , \mathcal{M} , f_{GW} , and d_L , and therefore only eight of these parameters are required to fully

describe the global CW signal. The following types of searches use a variety of prior setups to sample the necessary eight global parameters and are described below and summarized in Table 1. Including the necessary parameters to model the red noise in and distance to each of the 45 pulsars and model uncertainties in the solar system ephemeris with BayesEphem, there are 198 parameters in our all-sky MCMCs.

As in Aggarwal et al. (2019), to determine whether a CW has been detected by any of our analyses, we first performed a detection analysis with the priors described in Table 1, with the key difference between this and upper limit analyses being a log-uniform prior on the strain amplitude of the CW. Then, we calculated the Bayes factor using the Savage–Dickey formula (Dickey 1971),

$$\mathcal{B}_{10} \equiv \frac{\text{evidence}[\mathcal{H}_1]}{p(h_0 = 0|\mathcal{D}, \mathcal{H}_1)} \text{evidence} [\mathcal{H}_0] = \frac{p(h_0 = 0|\mathcal{H}_1)}{p(h_0 = 0|\mathcal{D}, \mathcal{H}_1)}.$$
(16)

Here \mathcal{H}_1 is the model with a CW, \mathcal{H}_0 is the model without one, $p(h_0 = 0|\mathcal{H}_1)$ is the prior at $h_0 = 0$, and $p(h_0 = 0|\mathcal{D}, \mathcal{H}_1)$ is the posterior at $h_0 = 0$. Since \mathcal{H}_1 and \mathcal{H}_0 are nested models (i.e., \mathcal{H}_0 is \mathcal{H}_1 : $h_0 = 0$), we used the Savage–Dickey formula to estimate $p(h_0 = 0|\mathcal{D}, \mathcal{H}_1)$ as the average fraction of samples in the lowest-amplitude bin in a histogram of h_0 samples for a range of bin sizes. We then computed the 1σ error on the Bayes factor as

$$\sigma = \frac{\mathcal{B}_{10}}{\sqrt{n}},\tag{17}$$

where *n* is the number of samples in the lowest-amplitude bin. As with the Bayes factor values, the average error is computed for a range of histogram bin sizes.

Throughout this work, we computed 95% upper limits as the 95th percentile of relevant strain (or chirp mass, for multimessenger analyses) posterior distributions. For these analyses, a uniform prior on the strain amplitude is used, which translates to a linear-exponential (LinExp) prior on $\log_{10} h$. The error on the 95% upper limit, due to the finite number of samples, is calculated as

$$\sigma_{\rm UL} = \frac{\sqrt{x(1-x)/N_s}}{p(h_0 = h_0^{95\%} | \mathcal{D})},\tag{18}$$

where x = 0.95 and N_s is the number of effective samples in the MCMC chain.

2.3.1. All-sky Searches

To search for GWs from SMBHBs located in any direction, we use uniform priors on the source sky position $(\cos \theta, \phi)$, as well as the cosine of the source inclination $\cos \iota$, polarization angle ψ , and GW phase Φ_0 . We used log-uniform priors on h_0 for detection analyses and uniform priors on h_0 for upper limit analyses, so as to set the most conservative upper limit. For both analysis types, priors on $\log_{10}(h_0)$ span the range [-18, -11], which accounts for an overconservative range around the sensitivity of the most recent data sets (order -15), and the minimum of which is well below our sensitivity.

We performed many searches at fixed values of f_{GW} , to evaluate detection statistics and our sensitivity across the entire nanohertz GW band. The lowest frequency value was set by the

Analysis Type	All-Sky		Sky Map	Targeted	
	Detection	Upper Limit	Upper Limit	Detection	Upper Limit
CRN	Y/N	Y/N	Y	Y/N	Y/N
log ₁₀ h	Uniform(-18,-11)	LinExp(-18,-11)	LinExp(-18,-11)		
$\log_{10} \mathcal{M}$	Uniform(7, \mathcal{M}_{max})	Uniform(7, \mathcal{M}_{max})	Uniform(7, \mathcal{M}_{max})	Uniform(7, \mathcal{M}_{max})	$LinExp(7, \mathcal{M}_{max})$
$\log_{10} d_L$				Constant	Constant
$\log_{10} f_{\rm GW}$	Constant (many)	Constant (many)	Constant (single)	Constant	Constant
ϕ	Uniform($0,2\pi$)	Uniform($0,2\pi$)	Uniform(pixel)	Constant	Constant
$\cos \theta$	Uniform(-1,1)	Uniform(-1,1)	Uniform(pixel)	Constant	Constant
ψ	Uniform $(0,\pi)$	Uniform $(0,\pi)$	Uniform $(0,\pi)$	Uniform $(0,\pi)$	Uniform $(0,\pi)$
Φ_0	Uniform $(0,2\pi)$	Uniform($0,2\pi$)	Uniform $(0,2\pi)$	Uniform $(0,2\pi)$	Uniform $(0,2\pi)$
$\cos \iota$	Uniform(-1,1)	Uniform(-1,1)	Uniform(-1,1)	Uniform(-1,1)	Uniform(-1,1)

 Table 1

 CW Parameter Priors for Each Analysis

time span of our data set, $f_{GW} = 1/(12.9 \text{ yr}) = 2.45 \times 10^{-9} \text{ Hz}.$ The highest frequency value is limited by the observation cadence of our data (approximately one observation per 2-4 weeks). However, SMBHBs at that frequency, at the mass range where their strains would be large enough to be detectable by PTAs, have exceedingly short inspiral timescales (from a few weeks up to \sim 3 months). Thus, they are unlikely to be detectable in our data set owing to rapid evolution, and therefore low residence times, at these frequencies, coupled with decreasing sensitivity of the PTA with increasing GW frequency caused by white noise (Islo et al. 2019; Aggarwal et al. 2020). Therefore, we set our maximum frequency to 3.178×10^{-7} Hz (equivalent to one GW cycle every ~36 days and a GW inspiral time of \sim 34 days). This is the same highfrequency cutoff value used in Arzoumanian et al. (2014) and Aggarwal et al. (2019).

For most of the frequency band, we searched over $\log_{10}(\mathcal{M}/M_{\odot})$ with a log-uniform prior with a range of [7, 10]. However, for very high frequency sources, we limit the maximum value of the prior to account for high chirp mass binaries never emitting GWs at the highest frequencies in our band, as they will have merged prior to emitting GWs at the searched frequency. This cutoff is relevant at $f_{\rm GW} \ge 1.913 \times 10^{-7}$ Hz. Assuming that binaries merge when the orbital frequency is equal to the innermost stable circular orbit (ISCO) frequency, \mathcal{M} must satisfy

$$\mathcal{M}_{\max} \leqslant \frac{1}{6^{3/2} \pi f_{\text{GW}}} \left[\frac{q}{(1+q)^2} \right]^{3/5},$$
 (19)

where *q* is the SMBHB mass ratio. Here we calculated the chirp mass cutoff for q = 1.

2.3.2. Sky Map

Due to the nonuniform distribution of pulsars on the sky, the NANOGrav PTA is not equally sensitive in all directions. To analyze the differences in sensitivity, once detection analyses were completed, we placed upper limits on 768 pixels distributed isotropically across the sky using healpy (Górski et al. 2005; Zonca et al. 2019); each pixel covers an area of 53.72 deg². This value is chosen to balance healpy's requirements for map transformations with our desired resolution. These settings allow us to resolve details on the sky sensitivity map but not overwhelm our computational capabilities of PTAs (Sesana & Vecchio 2010). We allowed the

sampler to search a uniform prior across each of the 768 pixels, so as to still sample the entire sky across the entire analysis.

Due to the large computational cost required to conduct 768 independent runs, the sky map is created at only a single frequency, and only upper limits are computed. We selected 7.65×10^{-9} Hz, as it was the most sensitive in the sky-averaged analysis. As this is in the low-frequency regime where we expect the inclusion of the CRN to be significant, it is included in our signal model. All other modeling is done identically to Section 2.3.1 and is summarized in Table 1.

2.3.3. Targeted Search

In addition to the two variations of searches described above, we also perform a targeted search for two known SMBHB candidates, 3C 66B and HS 1630+2355. Rather than a search for a generic SMBHB within a nearby galaxy cluster, as was done in Aggarwal et al. (2019) and Arzoumanian et al. (2021b), here we targeted these binary candidates directly. 3C 66B was the subject of Arzoumanian et al. (2020b) and was first identified because of observed orbital motion in the active galactic nucleus core (Sudou et al. 2003). Here we were able to provide an updated analysis with the addition of new data included in the 12.5 yr data set. HS 1630+2355 was first identified as a periodic quasar in Graham et al. (2021) owing to its location near our best-timed pulsars.

For the targeted search, we perform detection and upper limit analyses in the same way as in Section 2.3.1, with a few differences in the model priors. Because we know the sky location and luminosity distance to 3C 66B, as well as a frequency estimate, these parameters are set to constants in this search. This allows us to place constraints directly on the (observer-frame) chirp mass of the binary, rather than its GW strain amplitude. For a detection analysis the prior on $\log_{10}(\mathcal{M}/M_{\odot})$ is log-uniform in the range [7, 10], while for upper limit analyses the prior is uniform over this range. The remaining priors are identical to the above analyses and are summarized in Table 1.

2.3.4. Pulsar Distance Priors

In this work, we adopted a data-driven approach to handle the large uncertainties on pulsar distance measurements, which, in addition to a phase at each pulsar, affect the modeling of the pulsar terms of the CW signal. As in previous searches, the pulsar distance was used as a free parameter in the search. This allowed us to marginalize over the pulsar distance and avoid incorrect modeling of the signal at the location of the pulsar. Without such modeling, we would be required to dramatically increase our prior volume to allow the pulsar distances to vary across galactic scales, or, if the incorrect value were assumed, risk losing our chance at detecting the pulsar term of the CW signal. This is particularly critical at high GW frequencies, where sources evolve significantly between the Earth and pulsar terms.

In previous versions of this search (e.g., Aggarwal et al. 2019; Arzoumanian et al. 2020b), the pulsar distance prior was constructed from a Gaussian scaled to the parallax distance and associated uncertainty listed in Verbiest et al. (2012); if no distance was listed, a value of 1.0 ± 0.2 kpc was assumed. While this assumption is reasonable while placing upper limits (see discussion within Arzoumanian et al. 2020b), as the PTA reaches sensitivities where a detection is nearly possible, an improvement was needed.

In this work, every pulsar distance prior was constructed from a measurement or estimate. If a pulsar had a significant independent parallax measurement,⁵⁰ such as from very long baseline interferometry, or timing parallax measured in the 12.5 yr data set, this value was used to construct a prior on pulsar distance (L),

$$p(L) = \frac{1}{\sqrt{2\pi}\sigma_{\varpi}L^2} \exp\left[\frac{-(\mathrm{PX} - L^{-1})^2}{2\sigma_{\varpi}^2}\right],$$
 (20)

which inverts the approximately Gaussian shape of a parallax prior to describe the prior for distance (Vigeland & Vallisneri 2014). Here significance was defined by the parallax measurement (ϖ) having an associated uncertainty (σ_{ϖ}) of less than 30%, so as to avoid the introduction of any errors due to the Lutz–Kelker bias (Lutz & Kelker 1973). If multiple measurements of sufficient quality existed, these values and uncertainties were combined with a weighted average before being used to construct the parallax distance prior, which ensures that the highest-quality measurements contribute the most to the resulting prior.

If there are no parallax measurements that could be used to calculate the pulsar's distance, the pulsar's dispersion measure (DM) was used to construct a distance estimate using NE2001 (Cordes & Lazio 2002) and, subsequently, the distance prior. Since these values are only an estimate, we constructed a broad, nearly uniform prior for the DM–distance value and a 20% uncertainty (Cordes & Lazio 2002; Lam et al. 2016; Jones et al. 2017), with the shape

$$p(L) = \begin{cases} \text{Half} - \text{Gaussian} & \text{if } L < 0.8 L_{\text{DM}} \\ \text{Uniform} & \text{if } 0.8 L_{\text{DM}} \leqslant L \leqslant 1.2 L_{\text{DM}}. \\ \text{Half} - \text{Gaussian} & \text{if } L > 1.2 L_{\text{DM}} \end{cases}$$
(21)

Here the half-Gaussian additions have standard deviations of one-quarter of the DM-distance uncertainty. Unlike a sharp boundary, these additions allowed the sampler to move into the edges of this prior range, which accounted for any differences in distance estimates by alternative electron density models, such as Yao et al. (2017). While pulsar distance priors will still only induce minor influences on the results of an upper limit analysis (Arzoumanian et al. 2020b), by constructing new priors to accurately handle pulsar distance measurements and estimates, we have prepared our methods for a future detection of a CW, which will be more reliant on the pulsar term of the signal than upper limit evaluations. These values and the priors used are compiled in Table 2.

3. Results

3.1. All-sky Searches

For each GW frequency in our search, we performed a detection analysis on the 12.5 yr data that marginalized over the source sky location. Figure 1 shows the Bayes factor for a CW at each searched GW frequency in purple. It is important to note that the Bayes factor for $f_{\rm GW} = 2.45 \times 10^{-9}$ Hz (the lowest frequency analyzed) was undefined, with a steady decrease in the following four frequency bins. Ordinarily, a very large (or undefined) Bayes factor would be a first indication for the detection of a CW. However, given the strong evidence for the existence of a CRN process in the 12.5 yr data set (Arzoumanian et al. 2020a), it is clear that this signal appears to be of similar form, that is, what we have detected is bright at low frequencies and declines toward higher frequency. Once a CRN process is added to the model, with the $log_{10}A_{CRN}$ and $\gamma_{\rm CRN}$ parameters fixed to the maximum likelihood values (-15.80 and 6.08, respectively) found by a search analogous to Arzoumanian et al. (2020a), the Bayes factors for a CW at low $f_{\rm GW}$ return to <1 (leftmost red points in the figure). Therefore, throughout this paper we will present the results of many analyses with a fixed CRN included in our model. To constrain the initially undefined Bayes factor at $f_{GW} = 2.45$ nHz, we adapt the methodology described in Chatziioannou et al. (2014) to use a second MCMC analysis to "zoom in" on the low end of the strain prior range by limiting the prior to the 10th percentile of the original posterior. Therefore, the posterior height at $h_0 = 0$ becomes

$$p(h_0 = 0|\mathcal{D}, \mathcal{H}_1) = \frac{n_2}{N_2} \frac{n_1}{N_1} \frac{1}{dh},$$
 (22)

with fractional uncertainty

$$\sqrt{\frac{1}{n_1} + \frac{1}{n_2}},$$
 (23)

where N_1 is the number of samples in the initial run and n_1 is the number of samples in the focused region (defined as the 10th percentile of the initial run). Then, N_2 is the number of samples in the focused run, with n_2 of those samples located in the lowest-amplitude bin of width dh.

We note that a few frequencies above $f_{GW} = 1 \times 10^{-7}$ Hz have \mathcal{B}_{10} values that are returned as undefined. However, upon inspection, this is due to poor sampling in a few frequency bins, where the sampler does not explore low strain values, rather than a detection of a CW. This occurs in areas of parameter space where the likelihood is particularly complex and difficult to explore in a finite run time owing to the numerous complexities at $f_{GW} > 1 \times 10^{-7}$ Hz, such as covariances between the CW likelihood with pulsar binary orbits and potential unmodeled red noise above the 30-frequency

⁵⁰ http://hosting.astro.cornell.edu/research/parallax/, with values compiled from Ding et al. (2020), Jennings et al. (2018), Deller et al. (2019), Guillemot et al. (2016), Stovall et al. (2014), Abdo et al. (2013), Freire et al. (2012), Verbiest et al. (2009), Lazaridis et al. (2009), Chatterjee et al. (2009), Hotan et al. (2006), Lommen et al. (2006), Jacoby et al. (2005), Splaver et al. (2005), Löhmer et al. (2004), Toscano et al. (1999), Camilo et al. (1994).

 Table 2

 Compiled Pulsar Distance Values and Uncertainties for Each Pulsar Used in the 12.5 yr CW Analysis, Along with the Parallax (PX) or DM Prior Identifier

Pulsar	Prior	Distance (kpc)	Error (kpc)	Pulsar	Prior	Distance (kpc)	Error (kpc)
B1855+09	PX	1.4	0.24	B1937+21	РХ	3.55	0.64
B1953+29	DM	4.64	0.93	J0023+0923	PX	1.82	0.41
J0030+0451	PX	0.32	0.01	J0340+4130	DM	1.71	0.34
J0613-0200	PX	1.06	0.13	J0636+5128	PX	0.73	0.12
J0645+5158	PX	1.11	0.19	J0740+6620	DM	0.68	0.14
J0931-1902	DM	1.88	0.38	J1012+5307	PX	0.83	0.05
J1024-0719	PX	1.08	0.14	J1125+7819	DM	0.65	0.13
J1453+1902	DM	1.15	0.23	J1455-3330	PX	1.01	0.22
J1600-3053	PX	1.96	0.31	J1614-2230	PX	0.69	0.03
J1640+2224	DM	1.14	0.23	J1643-1224	PX	0.45	0.08
J1713+0747	PX	1.11	0.02	J1738+0333	PX	1.47	0.11
J1741+1351	PX	2.36	0.62	J1744-1134	PX	0.42	0.01
J1747-4036	DM	3.5	0.7	J1832-0836	PX	2.1	0.57
J1853+1303	DM	2.08	0.42	J1903+0327	DM	6.49	1.3
J1909-3744	PX	1.17	0.02	J1910+1256	DM	2.35	0.47
J1911+1347	DM	2.08	0.42	J1918-0642	PX	1.17	0.15
J1923+2515	DM	1.63	0.33	J1944+0907	DM	1.8	0.36
J2010-1323	PX	2.45	0.71	J2017+0603	DM	1.57	0.31
J2033+1734	DM	1.99	0.4	J2043+1711	PX	1.39	0.12
J2145-0750	PX	0.64	0.02	J2214+3000	DM	1.54	0.31
J2229+2643	DM	1.43	0.29	J2234+0611	PX	1.19	0.15
J2234+0944	DM	1.0	0.2	J2302+4442	DM	1.18	0.24
J2317+1439	PX	1.62	0.21				

Note. Values compiled using measurements from Ding et al. (2020), Jennings et al. (2018), Deller et al. (2019), Guillemot et al. (2016), Stovall et al. (2014), Abdo et al. (2013), Freire et al. (2012), Verbiest et al. (2009), Lazaridis et al. (2009), Chatterjee et al. (2009), Hotan et al. (2006), Lommen et al. (2006), Jacoby et al. (2005), Splaver et al. (2005), Löhmer et al. (2004), Toscano et al. (1999), Camilo et al. (1994), and Alam et al. (2021a).



Figure 1. Savage–Dickey Bayes factors for a CW at each GW frequency. At low frequencies, inclusion of a CRN in the model (filled red) is necessary to avoid a false CW detection as in the CW-only model (open purple). Squares indicate a frequency where the initial analysis returned an undefined Savage–Dickey Bayes Factor, meaning that the zoom-in analysis was necessary to calculate an accurate Bayes factor. With these methods, we found that no CWs are detected in the 12.5 yr data set. Key frequencies are marked by vertical lines, including f_{yr} (blue solid), $f_{max,RN} = 30/T_{obs}$ (black dotted), and $f_{max,CRN} = 5/T_{obs}$ (red dashed).

power-law cutoff (Chalumeau et al. 2022). Therefore, a few elevated Bayes factors are not unexpected. To mitigate this effect, we again apply the "zoom-in" methodology described above. After this procedure, all frequencies have Bayes factor values of $\mathcal{B}_{10} \lesssim 10$.

The only frequency that needed this treatment for both the CW and CW+CRN models is 1.763×10^{-7} Hz, which resulted in a Bayes factor of 15.43 in the CW+CRN case and 7.79 in the CW-only case. While we inspected our analyses at this frequency with extra care, these Bayes factors are still relatively

low compared to those required to claim a detection, especially since binaries at these high frequencies are expected to be quite rare (Kelley et al. 2018; Bécsy et al. 2022b). For comparison, evidence in favor of a given model is generally not considered strong for Bayes factors ≤ 100 (Kass & Raftery 1995). Therefore, we will monitor this frequency in future data sets, but currently our analyses indicate that no CWs are detected in the 12.5 yr data set.

As we found no strong evidence for a GW from an individual SMBHB in the 12.5 yr data set, we proceeded to place all-sky upper limits on the GW strain, with results shown in Figure 2. We again conduct this analysis using two different models, one that includes only a CW (purple) and one that includes both a CW and a CRN process (red). While in both cases the most sensitive frequency (that with the lowest strain upper limit) is 7.65×10^{-9} Hz, the strain upper limits are lower when the CRN is included in the model. In this case, we can limit the strain to $h_0 < (6.82 \pm 0.35) \times 10^{-15}$, whereas when the CRN is neglected, the best limit we can place on CW strain is $h_0 < (9.11 \pm 0.10) \times 10^{-15}$. This trend of the CW+CRN model resulting in lower upper limits than a CW-only model continues until frequencies of approximately 1×10^{-8} Hz, above which, where the effect of the power-law CRN is minimal, the upper limit values are nearly equal. Therefore, throughout the remainder of this work we opted to include the CRN in analyses that are too computationally expensive to be completed with both models, such as the sky map analyses described in Section 3.2. We note that we do not find a significantly higher upper limit at any of the frequencies where we found $\mathcal{B}_{10} \sim 10$ for either the CW or CW+CRN models: this indicates that the noise sources are decreasing the posterior



Figure 2. All-sky CW strain 95% upper limits and associated error regions, with (red) and without (purple) a CRN included in the model. At low frequencies, modeling the CRN is necessary to avoid overestimating our strain upper limits. We are the least sensitive to CWs at $f_{GW} = 1/(1 \text{ yr})$ owing to Earth's orbit, creating the large feature seen in this and other figures.

PDF at low strain amplitudes but not increasing the posterior PDF at the high strain amplitudes.

We are interested in looking at how our sensitivity to CWs changes as we increase the number of pulsars and extend the observing baseline. One approach is to perform "slice" analyses, where we truncate the data set to form shorter data sets and compare the upper limits from the sliced and full data sets (Hazboun et al. 2020). However, these sliced upper limits are not equivalent to previously published upper limits. Another approach is to directly compare this result to those of previous NANOGrav searches for CWs. In Figure 3, we compare this result to those of previous NANOGrav searches for CWs (Aggarwal et al. 2019). Direct comparisons between these data sets are complicated, due to the reprocessing of data resulting in new noise parameter values; nevertheless, such comparisons are useful to examine in order to understand how the sensitivity to CWs improves between data sets. While analyses have shown a factor of ~ 2 improvement between the previous three data sets, we see only a modest sensitivity improvement between the 11 and 12.5 yr data, with a difference of only 7% between the two lowest strain limits of $h_0 < (6.82 \pm 0.35) \times 10^{-15}$ (12.5 yr) and $h_0 < (7.33 \pm$ $(0.29) \times 10^{-15}$ (11 yr). In addition to the smaller fractional increase in observing baseline between the 11 and 12.5 yr data sets as compared to previous data sets, this is likely due to the presence of the CRN, which, while it is no longer causing a false positive in the CW search if included in the model, does represent a significant noise process that will limit our sensitivity to low-frequency CWs over the years to come (Hazboun et al. 2019b).

To confirm this hypothesis, we calculated the sensitivity curves of the 9, 11, and 12.5 yr data sets using each pulsar's red- and white-noise contributions and timing model with hasasia (Hazboun et al. 2019a, 2019b) and calculated the relative improvement in sensitivity between each data set at high frequencies ($>f_{yr}$), where red noise has little effect. We observed that on average the hasasia-calculated sensitivity at these frequencies improved by a factor of 1.28 between the 9 and 11 yr data sets and by a factor of 1.24 between the 11 and 12.5 yr data sets. In our full Bayesian analysis, our upper limits at frequencies above f_{vr} improved by a factor of 1.52 between



Figure 3. The upper limits on CW strain are continuing to decrease. The 12.5 yr data set (red curve and error region) is more sensitive than the 11, 9, and 5 yr data sets (blue, orange, and green curves, respectively) at high frequencies. At the most sensitive frequency of $f_{GW} = 7.65 \times 10^{-9}$ Hz, the CRN is impeding further sensitivity improvements, and upper limits are comparable between the 12.5 and 11 yr data sets. At frequencies greater than f_{yr} , NANOGrav's sensitivity has improved by a factor of 1.40 since the 11 yr data set.

the 9 and 11 yr data sets and by a factor of 1.40 between the 11 and 12.5 yr data sets. These proportionalities are even greater than our calculated improvements, so we are able to conclude that NANOGrav's sensitivity to CWs is improving as expected at high frequencies where red noise is not dominant.

3.2. Sky Map

In Figure 4, we show the GW strain upper limits for a model including a CRN at the most sensitive CW frequency $f_{\rm GW} = 7.65 \times 10^{-9}$ Hz as a function of sky location. As expected, the portion of the sky that is the least sensitive to CWs is that which contains the fewest pulsars. At the most sensitive pixel the strain upper limit is $h_0 < (2.66 \pm 0.15) \times 10^{-15}$, while at the least sensitive pixel $h_0 < (1.12 \pm 0.05) \times 10^{-14}$, a range of sensitivities that varies by a factor of ~4.

In Figure 5, we compare the 12.5 yr CW strain map to that constructed in Aggarwal et al. (2019) for the 11 yr data set by plotting $\Delta h_{95} = h_{95,12.5} - h_{95,11}$. While a portion (14%) of the sky shows a significant reduction in strain upper limits, 85% of our pixels show an increase in strain upper limit, indicating a



Figure 4. Map of CW strain 95% upper limits at $f_{GW} = 7.65 \times 10^{-9}$ Hz, the most sensitive frequency searched, for the 12.5 yr data set. Pulsar locations are shown as white stars, with new pulsars added from the 12.5 yr data set outlined in red. The most sensitive pixel is marked with a red circle and is located at an R.A. of $19^{h}07^{m}30^{s}$ and a decl. of $-30^{\circ}00'00''$. In this region, where our best-timed pulsars lie, our upper limits are nearly an order of magnitude more sensitive than the least sensitive pixel.



Figure 5. Difference in strain 95% upper limits for the 12.5 yr data set vs. the 11 yr data set at our most sensitive frequency. Blue pixels indicate a decrease in upper limit, while red pixels indicate an increase. The overall increase in upper limit across much of the sky at the most sensitive frequency was found to be due to the presence of the CRN and is consistent with the all-sky limit shown in Figure 3.

loss of sensitivity in the newest data set for much of the sky at our most sensitive frequency, including in the most sensitive area of the sky.

To investigate the cause of this apparent sensitivity loss, we conducted an analysis of the simulated data utilized in Pol et al. (2021). We selected portions of the data set with included pulsars and observation baselines corresponding to the 11 and 12.5 yr data sets that also included a CRN corresponding to that found in Arzoumanian et al. (2018). Then, we conducted upper limit analyses corresponding to the best-fit model for each data set (i.e., for a CW-only model for the 11 yr slice and a CW +CRN model for the 12.5 yr slice) for an equatorial slice of sky pixels (i.e., for the pixels with $\theta \sim \pi/2$). When plotted against ϕ in Figure 6, the patterns in Δh_{95} in the real data are well within the range represented by the same analysis in the 10 simulated data sets, each containing a different realization of the CRN. We observe that between 2h < RA < 8h, where NANOGrav has the fewest pulsars, the spread of upper limit



Figure 6. The difference in strain upper limits for an equatorial slice of the sky map shown in Figure 5 plotted against ϕ (or RA). The results for the real data (red points) are well within the range of values encompassed by the standard deviation of 10 realizations simulated (blue), with near-identical mean values of Δh_{95} (horizontal red and blue lines). Therefore, we conclude that the overall increase in upper limit across much of the sky at our most sensitive frequency is due to the 12.5 yr data set's sensitivity to the CRN.

difference values is by far the largest, which is consistent with our results. The mean value of Δh_{95} across each included pixel is nearly identical for the real data ($\overline{\Delta h_{95}} = 1.12 \times 10^{-15}$) and the simulations ($\overline{\Delta h_{95}} = 0.94 \times 10^{-15}$), and the real values are well within the intervals spanned by the 10 realizations. This indicates that the change in upper limits observed is likely a statistical fluctuation within the range of expected changes shown by our simulations. Together, this allows us to confidently state that while exact comparison between data sets is complex, this apparent pattern in our evolving sensitivity across the sky is due to the emerging CRN. This effect will have significant impacts on future PTA analyses and will be explored more extensively in future work (C. A. Witt & N. S. Pol 2023, in preparation).



Figure 7. The 95% lower limits on the luminosity distance to an individual SMBHB. While we can limit SMBHBs emitting GWs at the most sensitive value of $f_{\rm GW} = 7.65 \times 10^{-9}$ Hz to $d_L > 33.9$ Mpc, at $f_{\rm GW} = 3.82 \times 10^{-8}$ Hz they can be limited to farther away at $d_L > 35.0$ Mpc.

4. Astrophysical Limitations of Nearby SMBHBs

In recent years, numerous studies have modeled the SMBHB population in the nearby universe (Simon et al. 2014; Rosado & Sesana 2014; Schutz & Ma 2016; Mingarelli et al. 2017; Arzoumanian et al. 2021b), and multiple SMBHB candidates have been discovered with electromagnetic techniques (Sudou et al. 2003; Graham et al. 2015; Hu et al. 2020; Lehto & Valtonen 1996; Charisi et al. 2016; Liu et al. 2019). Even without a CW detection, our limits can add crucial insights into SMBHH populations, including limiting the distance to nearby SMBHBs and placing multimessenger mass constraints on SMBHB candidates.

4.1. Distance Limits

Our limits on CW strain can be transformed using Equation 15 to calculate the 95% lower limit on the luminosity distance to a source of a given chirp mass. The distance limits for an SMBHB with $\mathcal{M} = 10^9 M_{\odot}$ are shown in Figure 7. For the most sensitive frequency of $f_{\rm GW} = 7.65 \times 10^{-9}$ Hz, we can limit the distance to an SMBHB with $\mathcal{M} = 10^9 M_{\odot}$ to $d_L > 33.9$ Mpc. These limits may be scaled to larger or smaller SMBHBs directly using Equation (15) as

$$D_{95,\mathcal{M}} = D_{95,10^9 M_{\odot}} \times \left(\frac{\mathcal{M}}{10^9 M_{\odot}}\right)^{5/3}.$$
 (24)

However, it is important to note that while this frequency produces the lowest strain upper limit, it does not produce the farthest luminosity distance lower limit. This value is $d_L > 35.0$ Mpc at $f_{\text{GW}} = 3.82 \times 10^{-8}$ Hz.

This technique can be applied to the strain upper limit sky map as well, to calculate the 95% luminosity distance lower limit for an SMBHB emitting CWs at $f_{\rm GW} = 7.65 \times 10^{-9}$ Hz as a function of sky location. The results of this transformation are shown in Figure 8. At the most sensitive sky location, we can limit the minimum distance to an $\mathcal{M} = 10^9 M_{\odot}$ SMBHB to $d_L > 86.7$ Mpc and that to an $\mathcal{M} = 10^{10} M_{\odot}$ SMBHB to $d_L > 4.02$ Gpc. In the least sensitive sky location, we can limit the minimum distance to an $\mathcal{M} = 10^9 M_{\odot}$ SMBHB to $d_L > 20.5$ Mpc and that to an $\mathcal{M} = 10^{10} M_{\odot}$ SMBHB to $d_L > 0.95$ Gpc. These values vary by over a factor of 4 between the most and least sensitive parts of the sky.



Figure 8. Map of the 95% lower limit on the distance to individual SMBHBs with $\mathcal{M} = 10^9 M_{\odot}$ and 7.65×10^{-9} Hz. White diamonds indicate the positions of known SMBHB candidates and large galaxy clusters that could contain an SMBHB. As PTA sensitivities improve, these candidates may come into reach.

4.2. SMBHB Number Density Limits

Using our limits on the luminosity distance to an SMBHB, we can also place limits on the local number density of SMBHBs of a given binary configuration. After placing a lower limit on the effective comoving distance d_c to sources of given binary parameters, we can say that the local density is less than $n_c = 1/V_c = [(4/3)\pi d_c^3]^{-1}$. However, to consider this as a limit on the average density in some volume that is relatively local but larger than the explicitly measured volume, there should be some additional prefactor to account for the confidence of having a source within this volume based on Poisson distributions of sources. For a number of events $\Lambda = n_c V_c$ the likelihood of no detections is $P_0(\Lambda) = e^{-\Lambda}$. To find an upper limit on the occurrence rate, $\Lambda_{\text{UL}},$ we must integrate from that limit to infinity, such that the result matches our desired confidence level p_0 . Therefore, $F_{\rm UL}(\Lambda_{\rm UL}) =$ $\int_{\Lambda_{\rm III}}^{\infty} e^{-\Lambda} d\Lambda = 1 - p_0 \text{ is solved as}$

$$n_{ul} = \frac{-\ln(1 - p_0)}{V_c}.$$
 (25)

Here our desired confidence level is $p_0 = 0.95$. To calculate the comoving distance d_c , we transform our luminosity distance limits (shown in Figure 7) as $d_c = d_L/(1+z)$, and z is calculated for the relevant luminosity distance values using astropy.

The results of this calculation are shown for various SMBHB chirp masses in Figure 9. As can be expected, we find that we can place more constraining upper limits on large SMBHBs $(\mathcal{M} = 10^{9.5} M_{\odot})$ than smaller ones $(\mathcal{M} = 10^8 M_{\odot})$ in the local universe.

4.3. Multimessenger Analyses

Using the methodology described in Section 2.3.3, we conducted a multimessenger search for GWs from the SMBHB candidate 3C 66B to provide an update to the results of Arzoumanian et al. (2020b). The detection analyses result in nearly identical Savage–Dickey Bayes factors, whether the CRN was included or not. This is to be expected, as the CRN is very weak at frequencies as high as that of 3C 66B ($f_{\rm GW} = 6.04 \times 10^{-8}$ Hz). The Bayes factors for the CW-only analysis and the CW+CRN analysis are 0.70 ± 0.02 and



Figure 9. Number density limits of SMBHBs per comoving Mpc⁻³ in the local universe, where, as expected, we placed significantly more stringent upper limits on the largest SMBHBs than on the smallest ones, with limits decreasing from those on chirp masses of $10^8 M_{\odot}$ (purple) to $10^{8.5} M_{\odot}$ (blue) to $10^9 M_{\odot}$ (teal) to $10^{9.5} M_{\odot}$ (green).

 0.67 ± 0.01 , respectively. Both of these values are very near 1, meaning that the data do not indicate the presence of a CW corresponding to a binary within 3C 66B.

Because no GW was detected, we constrain the chirp mass of a potential binary with an upper limit analysis, again performed with and without a CRN to confirm consistency. The posteriors from these two searches are plotted in Figure 10, with resulting 95% upper limits of $\mathcal{M} < (1.41 \pm 0.02) \times 10^9 M_{\odot}$ when a CRN is included and $\mathcal{M} < (1.34 \pm 0.01) \times 10^9 \, M_{\odot}$ when only CWs are included in the signal. For comparison, the 95% chirp mass upper limit for 3C 66B from the 11 yr data set was $\mathcal{M} < 1.65 \times 10^9 \ M_{\odot}$. This represents an improvement of $2.4 \times 10^8 M_{\odot}$, or a factor of 1.2 smaller; by adding pulsars, extending timing baselines, and improving timing and searching methods, the PTA's sensitivity has clearly improved. These upper limits are nearer to the value of the upper bound of the Iguchi et al. (2010) chirp mass estimate. In subsequent data sets, or by using more sophisticated analyses such as advanced noise modeling (J. Simon & J. S. Hazboun 2023, in preparation), this error region may soon be within reach.

In Arzoumanian et al. (2020b), it was shown that a targeted search, like this analysis, results in a factor of ~2 reduction in upper limits compared to those of an all-sky search at a corresponding GW frequency. When converted to strain amplitudes rather than chirp masses, the 95% upper limits are $h_0 < 1.90 \times 10^{-14}$ and $h_0 < 1.74 \times 10^{-14}$ for the searches with and without a CRN, respectively. In comparison, the all-sky analysis in Section 3.1 returned strain upper limits of $h_0 < 3.56 \times 10^{-14}$ and $h_0 < 3.82 \times 10^{-14}$ at $f_{\rm GW} = 6.01 \times 10^{-8}$ Hz, the nearest frequency to that of 3C 66B at $f_{\rm GW} = 6.04 \times 10^{-8}$ Hz. These all-sky strain upper limits are a factor of 1.88 and 2.20 larger, very similar to the value for the 11 yr data set. Therefore, the improvement in upper limits gained by using this multimessenger technique has stayed stable across the addition of new pulsars, more data, and the emergence of the CRN.

Additionally, we performed a new search for the electromagnetic SMBHB candidate HS 1630+2355. First identified as a periodic quasar in Graham et al. (2015), this candidate is identified as a top PTA CW candidate in Xin et al. (2021) with a GW frequency of $f_{\rm GW} = 1.13 \times 10^{-8}$ Hz and a luminosity distance of 5.26 Gpc. In the 12.5 yr data set, we do not detect



Figure 10. Posterior distributions for a targeted upper limit analysis of the SMBHB candidate 3C 66B. While 95% upper limits (red and purple lines) are lower than in the 11 yr data set (blue line), they cannot rule out the model from Iguchi et al. (2010) (orange region).

any CWs from HS 1630+2355; in a CW+CRN analysis (necessary owing to the low GW frequency), we calculate a Bayes factor of 0.74 ± 0.02 . Then, we are able to set an upper limit of $\mathcal{M} < (1.28 \pm 0.03) \times 10^{10} M_{\odot}$ on the chirp mass of an SMBHB within HS 1630+2355, which corresponds to a strain of $h_0 < 4.03 \times 10^{-15}$. For comparison, the all-sky upper limit at the nearest frequency of $f_{\rm GW} = 1.10 \times 10^{-8}$ Hz is $h_0 < 1.07 \times 10^{-14}$, a factor of 2.66 larger than the targeted upper limit. Due to this candidate's favorable position near the PTA's most sensitive sky location, we are able to overcome the much larger source distance to set a constraining upper limit. However, this limit is still approximately 4 times larger than the estimated chirp mass of $3.15 \times 10^9 M_{\odot}$ (Xin et al. 2021), meaning that more data are needed to rule out or detect an SMBHB within HS 1630+2355. The simulations in Xin et al. (2021) indicate that HS 1630+2355 will not be detectable even by IPTA data sets by the late 2020s, so this result is unsurprising; therefore, HS 1630+2355 will require continued monitoring until PTA sensitivity brings it into reach.

4.4. Local Detection Prospects

At the most sensitive sky pixel, we conducted a final upper limit analysis across the entire frequency band, with results plotted in Figure 11. Here we observed that for all frequencies the PTA is dramatically more sensitive to CWs from sources at this sky location than across the entire sky on average. Mingarelli et al. (2017) carried out a comprehensive study of the detection prospects of SMBHBs within a 225 Mpc volume, the completeness limit for their chosen *K*-band luminosity in the Two Micron All Sky Survey. Using these new 12.5 yr upper limit curves, we assess our level of surprise at our current nondetection of CWs.

Figure 11 shows an example realization of the local SMBHB population created with nanohertz_gws (Mingarelli 2017). It is 1 out of 75,000 Monte Carlo realizations Mingarelli et al. (2017) carried out, where they varied black hole masses via the scatter in various $M - M_{bulge}$ relations, mass ratios, and more. While the chosen realization shows what a detectable SMBHB would look like, on average we found that only 398 realizations out of the 75,000 contained detectable SMBHB systems at the



Figure 11. The 95% strain upper limit curve for the all-sky (red solid) CW search compared with the 95% strain upper limit curve in the most sensitive sky location (red dashed). The nondetection of a nearby SMBHB is unsurprising—there was at best a 0.5% chance of making such a detection. Here we show one of the 75,000 realizations of the local universe from Mingarelli et al. (2017). This realization shows a detectable SMBHB, together with our 95% upper limit curves for both sky-averaged and best sky locations. In this realization there are 87 local SMBHBs (all within 225 Mpc); none of them lie above the sky-averaged upper limit curve, but one could be detected if it were at the most sensitive sky location.

best sky location. We therefore only had a 0.5% chance of making a detection of such a local source with the 12.5 yr data set. Furthermore, when we consider the entire sky, we found that an order of magnitude fewer SMBHBs were detectable—only 43 realizations contained detectable binaries.

It is interesting to compare this result to that of our previous upper limit (Aggarwal et al. 2019). With the NANOGrav 11 yr all-sky upper limits, we found 34 detectable SMBHBs, and here we find 43—an overall improvement. However, the upper limit at our best sky location has deteriorated owing to the CRN, which has in turn decreased the number of detectable binaries by a factor of \sim 2, from a 1.2% chance of detection to 0.5%.

As was the case in previous sections, we note that this comparison is nontrivial, due to the complex changes in sensitivity between data sets, and that this deterioration is happening primarily at low frequencies where the CRN is manifesting in the data and the most sensitive sky location is heavily affected (Figures 5 and 6). Xin et al. (2021) show that at higher GW frequencies the effect of the GWB, or any equivalent CRN, is very small, so the detection prospects for local SMBHBs are unaffected.

4.5. Binary Population Model Consistency

Finally, it was also useful to assess whether our current nondetection of CWs is consistent with expectations from SMBHB population models. In Figure 12 we compared an astrophysically motivated SMBHB model to GW upper limits set with the 12.5 yr CW search. The SMBHB model was derived from theoretical galaxy major merger rates (Chen et al. 2019), which are themselves based on observed galaxy pair fractions (Mundy et al. 2017) and theoretical galaxy merger timescales. It is related to the GWB via (Phinney 2001; Sesana 2013)

$$h_c^2(f) = \frac{4}{3\pi} \frac{1}{f^{4/3}} \iint \phi_{\rm BHB}(\mathcal{M}, z) \frac{\mathcal{M}^{5/3}}{(1+z)^{1/3}} d\mathcal{M} dz, \quad (26)$$

where h_c is the characteristic strain of the GWB and M is the chirp mass in the observer frame. This was fit to the results of



Figure 12. The SMBHB mass function (ϕ_{BHB}) derived from astrophysical models shows the modeled number density of SMBHBs (color bar) across log chirp mass $(\log_{10} M/M_{\odot})$ and redshift (z). Side panels show ϕ_{BHB} in one dimension integrated across each respective variable. Regions that are inconsistent with our 12.5 yr CW search are shown in white, with the all-sky (average) and most sensitive (best) sky location upper limits shown under the solid and dashed–dotted white curves, respectively. Created using methods from J. A. Casey-Clyde et al. (2023, in preparation).

the NANOGrav search for the GWB in the 12.5 yr data set (Arzoumanian et al. 2020a) and assumes that the CRN is due to a GWB, comparable to the fit in Middleton et al. (2021).

The GW limits in Figure 12 were calculated using the most sensitive frequency of both the all-sky and most sensitive sky location analyses. Figure 12 thus shows what regions of z-M parameter space were accessible to the 12.5 yr CW search. Since no CWs were detected, we are able to rule out the highmass and low-z region across the entire sky and at the most sensitive sky location for the PTA's most sensitive frequency.

We calculate the expected number of detectable SMBHBs by relating the differential SMBHB mass function ϕ_{BHB} to the differential number of binaries per chirp mass, frequency, and redshift (Sesana et al. 2008) as

$$\frac{d^3N}{d\log\mathcal{M}dzdf} = \frac{d^2\phi_{\rm BHB}}{d\log\mathcal{M}dz}\frac{dV}{dz}\frac{dz}{dt_r}\frac{dt_r}{df_r}\frac{df_r}{df}$$
(27)

and integrating across the relevant region of z-M space, while also considering the entire strain sensitivity curve in frequency space. Here t_r and f_r are the proper time and binary GW frequency in the SMBHB's rest frame, respectively. We find in both cases that the expected number of SMBHBs is $\ll 1$. At the all-sky sensitivity the calculated number is $0.6^{+1.1}_{-0.4} \times 10^{-4}$, while at the most sensitive sky location the calculated number is $8.6^{+12.9}_{-5.5} \times 10^{-4}$. Our nondetection of a CW signal is thus consistent with theoretical models of the SMBHB population, which predict that the most massive, and therefore loudest, SMBHBs are exceedingly rare.

5. Discussion and Future Prospects

While the NANOGrav PTA is continuing to increase our sensitivity to GWs by adding data from ongoing observations and adding new pulsars to the PTA, our limits on CW strains across the nanohertz GW frequency band and the sky have not improved as steadily as in previous data sets. This is due to the CRN first detected in the 12.5 yr data set in Arzoumanian et al. (2020a), which has impacted the PTA's ability to distinguish a CW source. While adding a CRN to the search model that is fixed to the maximum likelihood values from a dedicated search avoids confusion in detection analyses, this adds a significant source of noise to the PTA and therefore limits our sensitivity to CWs at frequencies below 10 nHz.

We have entered an interesting era where surprising results will continue to be uncovered. In future data sets, the CRN will likely be even more apparent in the data, and it may eventually resolve to be due to a stochastic GWB from SMBHBs (Pol et al. 2021). In any case, due to the multifrequency nature of the GWB, this will continue to impact CW searches, and significant efforts will be needed to continue development on methods that will allow for efficient detection of both types of nanohertz GW signals such as in Bécsy & Cornish (2020), as well as extensive simulations that evaluate detection possibilities, as in Pol et al. (2021), that include multiple types of GW signal in the simulated data sets. Additionally, significant effort will be needed to improve sampling methods that can efficiently explore the complex CW parameter space (Bécsy et al. 2022a), particularly at high GW frequencies or if full eccentricity modeling is desired (Taylor et al. 2016). These complexities will only be exacerbated as data sets expand, particularly for the complex data sets produced by the IPTA, which, while more sensitive, contain more pulsars and noise parameters over which to sample. One promising path forward are targeted searches of quasars, which may be much more likely to host SMBHBs than random galaxies (J. A. Casey-Clyde et al. 2023, in preparation). Since multimessenger analyses can improve upper limits by a factor of 2 (Arzoumanian et al. 2020b), improve detection prospects (Liu & Vigeland 2021; Charisi et al. 2022), and can be made drastically more efficient than traditional all-sky searches (Charisi et al. 2022), further development of these methods is also crucial, as with more data electromagnetic SMBHB candidates may soon be detectable (Xin et al. 2021), and many more will be identified in upcoming surveys (Charisi et al. 2022; Witt et al. 2022). By balancing these efforts, a CW signal may soon come into reach.

6. Conclusions

With extensive Bayesian analyses, we have searched the NANOGrav 12.5 yr data set for CWs from individual SMBHBs. In our detection analyses, we showed that no CWs were detected to a high degree of confidence. We then placed all-sky upper limits on the strain amplitude for all CWs emitting between 2.45×10^{-9} Hz and 3.19×10^{-7} Hz, as well as upper limits as a function of sky location for the 12.5 yr data set's most sensitive frequency of 7.65×10^{-9} Hz.

This analysis also included the development of new methods to accurately reflect the realistic distribution of possible values of pulsar distances from updated measurements. The way we treat these values in search pipelines has a significant impact on our ability to detect the pulsar term of a CW signal, and these methods will be critical as we proceed toward PTA sensitivities that enable a CW detection.

Unlike previous data sets, the 12.5 yr data set contains a significant CRN. Therefore, for the first time, we included the CRN in our Bayesian searches by fixing the model parameters to those recovered in Arzoumanian et al. (2020a). This had a significant effect on the results of many of our analyses and

proved critical to avoid a false detection of a CW at 2.45×10^{-9} Hz. This process also significantly impeded the reduction of our upper limits between the 11 and 12.5 yr NANOGrav searches at the most sensitive frequency of 7.65×10^{-9} Hz in most areas of the sky. The presence of a CRN will also impact searches for other types of signals, such as bursts with memory and fuzzy dark matter, and so searches for those sources will also need to include the CRN.

Despite these new necessities, we are able to place significant astrophysical constraints on the local SMBHB population. In our most sensitive sky location, we can rule out the existence of any SMBHB with a mass of at least $10^9 M_{\odot}$ emitting at 7.65×10^{-9} Hz within 86.7 Mpc. Furthermore, we demonstrate that significant improvements to chirp mass upper limits of SMBHB candidates can be made through multimessenger analysis techniques, and we limit the chirp mass of 3C 66B to $\mathcal{M} < (1.34 \pm 0.01) \times 10^9 M_{\odot}$. With the inclusion of more data, we will soon be able to rule out or confirm this source and other binary candidates, as well as those that are yet undiscovered.

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Author contributions

An alphabetical-order author list was used for this paper in recognition of the fact that a large, decade-timescale project such as NANOGrav is necessarily the result of the work of many people. All authors contributed to the activities of the NANOGrav Collaboration leading to the work presented here and reviewed the manuscript, text, and figures prior to the paper's submission. Additional specific contributions to this paper are as follows. Z.A., H.B., P.R.B., H.T.C., M.E.D., P.B. D., T.D., J.A.E., R.D.F., E.C.F., E.F., N.G.-D., P.A.G., D.C.G., M.L.J., M.T.L., D.R.L., R.S.L., J.L., M.A.M., C.N., D.J.N., T. T.P., N.S.P., S.M.R., K.S., I.H.S., R.S., J.K.S., R.S., and S.J.V. developed the 12.5 yr data set through a combination of observations, arrival-time calculations, data checks and refinements, and timing model development and analysis; additional specific contributions to the data set are summarized in Alam et al. (2021a). C.A.W. coordinated the writing of the paper and led the search. B.B., A.R.K., N.S.P., J.Sy., G.W., and C.A.W. performed analyses for the project, including exploratory runs. J.S. and C.A.W. developed methods to include the CRN in the search model. A.B., N.G.-D., J.G., K.G., S.R.T., S.J.V., and C.A.W. proposed for the necessary XSEDE resources to complete these analyses. N.S.P. and C.A.W. performed the sky map simulations. A.C.-C., L.Z.K., C.M.F.M., and C.A.W. developed the astrophysical interpretations. A.D.J. provided updates to red-noise empirical distributions. G.E.F., X.S., and S.J.V. explored the frequentist analyses. S.C., D.J.N., M.A.M., and C.A.W. updated the pulsar distance priors. S.B.S., C.M.F. M., and C.A.W. wrote the manuscript and produced the figures. We thank B.B., S.C., J.M.C., N.J.C., W.F., K.G., J.S.H., D.L. K., L.Z.K., M.T.L., T.J.W.L., M.A.M., D.J.N., K.D.O., J.D.R., S.R.T., and S.J.V. for their thoughtful comments on the manuscript.

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References

- Abdo, A. A., Ajello, M., Allafort, A., et al. 2013, ApJS, 208, 17
- Aggarwal, K., Arzoumanian, Z., Baker, P. T., et al. 2019, ApJ, 880, 116
- Aggarwal, K., Arzoumanian, Z., Baker, P. T., et al. 2020, ApJ, 889, 38
- Alam, M. F., Arzoumanian, Z., Baker, P. T., et al. 2021a, ApJS, 252, 4
- Alam, M. F., Arzoumanian, Z., Baker, P. T., et al. 2021b, ApJS, 252, 5
- Antoniadis, J., Arzoumanian, Z., Babak, S., et al. 2022, MNRAS, 510, 4873
- Arzoumanian, Z., Baker, P. T., Blumer, H., et al. 2020a, ApJL, 905, L34
- Arzoumanian, Z., Baker, P. T., Blumer, H., et al. 2021a, PhRvL, 127, 251302
- Arzoumanian, Z., Baker, P. T., Brazier, A., et al. 2018, ApJ, 859, 47 Arzoumanian, Z., Baker, P. T., Brazier, A., et al. 2020b, ApJ, 900, 102
- Arzoumanian, Z., Baker, P. T., Brazier, A., et al. 2021b, ApJ, 914, 121
- Arzoumanian, Z., Brazier, A., Burke-Spolaor, S., et al. 2014, ApJ, 794, 141
- Arzoumanian, Z., Brazier, A., Burke-Spolaor, S., et al. 2016, ApJ, 821, 13
- Astropy Collaboration, Robitaille, T. P., Tollerud, E. J., et al. 2013, A&A, 558, A33
- Babak, S., Petiteau, A., Sesana, A., et al. 2016, MNRAS, 455, 1665
- Bécsy, B., & Cornish, N. J. 2020, CQGra, 37, 135011
- Bécsy, B., Cornish, N. J., & Digman, M. C. 2022a, PhRvD, 105, 122003
- Bécsy, B., Cornish, N. J., & Kelley, L. Z. 2022b, ApJ, 941, 119
- Begelman, M. C., Blandford, R. D., & Rees, M. J. 1980, Natur, 287, 307
- Benetti, M., Graef, L. L., & Vagnozzi, S. 2022, PhRvD, 105, 043520
- Burke-Spolaor, S., Taylor, S. R., Charisi, M., et al. 2019, A&ARv, 27, 5
- Camilo, F., Foster, R. S., & Wolszczan, A. 1994, ApJL, 437, L39
- Chalumeau, A., Babak, S., Petiteau, A., et al. 2022, MNRAS, 509, 5538
- Charisi, M., Bartos, I., Haiman, Z., et al. 2016, MNRAS, 463, 2145
- Charisi, M., Taylor, S. R., Runnoe, J., Bogdanovic, T., & Trump, J. R. 2022, INRAS, 510, 5929
- Chatterjee, S., Brisken, W. F., Vlemmings, W. H. T., et al. 2009, ApJ, 698, 250 Chatziioannou, K., Cornish, N., Klein, A., & Yunes, N. 2014, PhRvD, 89, 104023
- Chen, S., Caballero, R. N., Guo, Y. J., et al. 2021, MNRAS, 508, 4970
- Chen, S., Sesana, A., & Conselice, C. J. 2019, MNRAS, 488, 401
- Cordes, J. M., & Lazio, T. J. W. 2002, arXiv:astro-ph/0207156
- Deller, A. T., Goss, W. M., Brisken, W. F., et al. 2019, ApJ, 875, 100
- Demorest, P. B., Ferdman, R. D., Gonzalez, M. E., et al. 2013, ApJ, 762, 94
- Desvignes, G., Caballero, R. N., Lentati, L., et al. 2016, MNRAS, 458, 3341 Detweiler, S. 1979, ApJ, 234, 1100
- Dickey, J. M. 1971, Ann. Math. Stat., 42, 204
- Ding, H., Deller, A. T., Freire, P., et al. 2020, ApJ, 896, 85
- Ellis, J., & van Haasteren, R. 2017, Jellis18/Ptmcmcsampler: Official Release, v1.0.0, Zenodo, doi:10.5281/zenodo.1037579
- Ellis, J. A., Siemens, X., & Creighton, J. D. E. 2012, ApJ, 756, 175
- Ellis, J. A., Vallisneri, M., Taylor, S. R., & Baker, P. T. 2019, ENTERPRISE: Enhanced Numerical Toolbox Enabling a Robust PulsaR Inference SuitE, ascl:1912.015
- Falxa, M., Babak, S., Baker, P. T., et al. 2023, MNRAS, 521, 5077

- Folkner, W. M., & Park, R. S. 2018, Planetary ephemeris DE438 for Juno, Tech. Rep. IOM 392R-18-004, Jet Propulsion Laboratory, Pasadena, CA Foster, R. S., & Backer, D. C. 1990, ApJ, 361, 300
- Freire, P. C. C., Wex, N., Esposito-Farèse, G., et al. 2012, MNRAS, 423, 3328
- Goncharov, B., Shannon, R. M., Reardon, D. J., et al. 2021, ApJL, 917, L19
- Goncharov, B., Thrane, E., Shannon, R. M., et al. 2022, ApJL, 932, L22
- Górski, K. M., Hivon, E., Banday, A. J., et al. 2005, ApJ, 622, 759
- Graham, M. J., Djorgovski, S. G., Stern, D., et al. 2015, MNRAS, 453, 1562
- Guillemot, L., Smith, D. A., Laffon, H., et al. 2016, A&A, 587, A109
- Hazboun, J., Romano, J., & Smith, T. 2019a, JOSS, 4, 1775
- Hazboun, J. S., Romano, J. D., & Smith, T. L. 2019b, PhRvD, 100, 104028 Hazboun, J. S., Simon, J., Taylor, S. R., et al. 2020, ApJ, 890, 108
- Hobbs, G. 2013, CQGra, 30, 224007
- Hobbs, G. B., Edwards, R. T., & Manchester, R. N. 2006, MNRAS, 369, 655
- Hotan, A. W., Bailes, M., & Ord, S. M. 2006, MNRAS, 369, 1502
- Hu, B. X., D'Orazio, D. J., Haiman, Z., et al. 2020, MNRAS, 495, 4061
- Hunter, J. D. 2007, CSE, 9, 90
- Iguchi, S., Okuda, T., & Sudou, H. 2010, ApJL, 724, L166
- Islo, K., Simon, J., Burke-Spolaor, S., & Siemens, X. 2019, arXiv:1906.11936
- Jacoby, B. A., Hotan, A., Bailes, M., Ord, S., & Kulkarni, S. R. 2005, ApJL, 629, L113
- Jenet, F. A., Lommen, A., Larson, S. L., & Wen, L. 2004, ApJ, 606, 799
- Jennings, R. J., Kaplan, D. L., Chatterjee, S., Cordes, J. M., & Deller, A. T. 2018, ApJ, 864, 26
- Jones, M. L., McLaughlin, M. A., Lam, M. T., et al. 2017, ApJ, 841, 125
- Kass, R. E., & Raftery, A. E. 1995, JASA, 90, 773
- Kelley, L. Z., Blecha, L., Hernquist, L., Sesana, A., & Taylor, S. R. 2018, MNRAS, 477, 964
- Kerr, M., Reardon, D. J., Hobbs, G., et al. 2020, PASA, 37, e020
- Lam, M. T., Cordes, J. M., Chatterjee, S., et al. 2016, ApJ, 821, 66
- Lam, M. T., Cordes, J. M., Chatterjee, S., et al. 2017, ApJ, 834, 35
- Lazaridis, K., Wex, N., Jessner, A., et al. 2009, MNRAS, 400, 805 Lehto, H. J., & Valtonen, M. J. 1996, ApJ, 460, 207
- Lentati, L., Taylor, S. R., Mingarelli, C. M. F., et al. 2015, MNRAS, 453, 2576
- Liu, T., Gezari, S., Ayers, M., et al. 2019, ApJ, 884, 36
- Liu, T., & Vigeland, S. J. 2021, ApJ, 921, 178
- Löhmer, O., Kramer, M., Driebe, T., et al. 2004, A&A, 426, 631 Lommen, A. N., & Backer, D. C. 2001, ApJ, 562, 297
- Lommen, A. N., Kipphorn, R. A., Nice, D. J., et al. 2006, ApJ, 642, 1012
- Luo, J., Ransom, S., Demorest, P., et al. 2019, PINT: High-precision pulsar timing analysis package, Astrophysics Source Code Library, ascl:1902.007 Lutz, T. E., & Kelker, D. H. 1973, PASP, 85, 573
- McLaughlin, M. A. 2013, CQGra, 30, 224008
- Middleton, H., Sesana, A., Chen, S., et al. 2021, MNRAS, 502, L99
- Mingarelli, C. 2017, ChiaraMingarelli/nanohertz_GWs: First release!, v1.0, Zenodo, doi:10.5281/zenodo.838712
- Mingarelli, C. M. F., Lazio, T. J. W., Sesana, A., et al. 2017, NatAs, 1, 886
- Mundy, C. J., Conselice, C. J., Duncan, K. J., et al. 2017, MNRAS, 470, 3507
- Nice, D., Demorest, P., Stairs, I., et al. 2015, Tempo: Pulsar timing data analysis, Astrophysics Source Code Library, ascl:1509002
- Perera, B. B. P., DeCesar, M. E., Demorest, P. B., et al. 2019, MNRAS, 490, 4666
- Phinney, E. S. 2001, arXiv:astro-ph/0108028
- Pol, N. S., Taylor, S. R., Kelley, L. Z., et al. 2021, ApJL, 911, L34
- Price-Whelan, A. M., Sipőcz, B. M., Günther, H. M., et al. 2018, AJ, 156, 123
- Rosado, P. A., & Sesana, A. 2014, MNRAS, 439, 3986
- Rosado, P. A., Sesana, A., & Gair, J. 2015, MNRAS, 451, 2417
- Schutz, K., & Ma, C.-P. 2016, MNRAS, 459, 1737
- Sesana, A. 2013, MNRAS, 433, L1

extensions

817.70

16

- Sesana, A., Haardt, F., Madau, P., & Volonteri, M. 2004, ApJ, 611, 623
- Sesana, A., & Vecchio, A. 2010, PhRvD, 81, 104008
- Sesana, A., Vecchio, A., & Colacino, C. N. 2008, MNRAS, 390, 192
- Shannon, R. M., & Cordes, J. M. 2010, ApJ, 725, 1607
- Shannon, R. M., Ravi, V., Coles, W. A., et al. 2013, Sci, 342, 334
- Shannon, R. M., Ravi, V., Lentati, L. T., et al. 2015, Sci, 349, 1522

Stovall, K., Lynch, R. S., Ransom, S. M., et al. 2014, ApJ, 791, 67

Sudou, H., Iguchi, S., Murata, Y., & Taniguchi, Y. 2003, Sci, 300, 1263

- Simon, J., Polin, A., Lommen, A., et al. 2014, ApJ, 784, 60
- Splaver, E. M., Nice, D. J., Stairs, I. H., Lommen, A. N., & Backer, D. C. 2005, ApJ, 620, 405

Taylor, S. R., Baker, P. T., Hazboun, J. S., Simon, J., & Vigeland, S. J. 2021,

Taylor, S. R., Huerta, E. A., Gair, J. R., & McWilliams, S. T. 2016, ApJ,

Toscano, M., Britton, M. C., Manchester, R. N., et al. 1999, ApJL, 523, L171

enterprise_extensions, v2.4.3, https://github.com/nanograv/enterprise_

- Towns, J., Cockerill, T., Dahan, M., et al. 2014, CSE, 16, 62
- Vagnozzi, S. 2021, MNRAS, 502, L11
- Vallisneri, M. 2020, libstempo: Python wrapper for Tempo2, Astrophysics Source Code Library, ascl:2002.017
- Vallisneri, M., Taylor, S. R., Simon, J., et al. 2020, ApJ, 893, 112
- van Haasteren, R., Levin, Y., Janssen, G. H., et al. 2011, MNRAS, 414, 3117
- Verbiest, J. P. W., Bailes, M., Coles, W. A., et al. 2009, MNRAS, 400, 951
- Verbiest, J. P. W., Lentati, L., Hobbs, G., et al. 2016, MNRAS, 458, 1267
- Verbiest, J. P. W., Weisberg, J. M., Chael, A. A., Lee, K. J., & Lorimer, D. R. 2012, ApJ, 755, 39

- Vigeland, S. J., Islo, K., Taylor, S. R., & Ellis, J. A. 2018, PhRvD, 98, 044003
- Vigeland, S. J., & Vallisneri, M. 2014, MNRAS, 440, 1446
- Witt, C. A., Charisi, M., Taylor, S. R., & Burke-Spolaor, S. 2022, ApJ, 936, 89
- Xin, C., Mingarelli, C. M. F., & Hazboun, J. S. 2021, ApJ, 915, 97
- Xue, X., Bian, L., Shu, J., et al. 2021, PhRvL, 127, 251303
- Yao, J. M., Manchester, R. N., & Wang, N. 2017, ApJ, 835, 29
- Yardley, D. R. B., Hobbs, G. B., Jenet, F. A., et al. 2010, MNRAS, 407, 669
- Zhu, X.-J., Hobbs, G., Wen, L., et al. 2014, MNRAS, 444, 3709 Zic, A., Hobbs, G., Shannon, R. M., et al. 2022, MNRAS, 516, 410
- Zonca, A., Singer, L., Lenz, D., et al. 2019, JOSS, 4, 1298

17